

# Ownership, Pointer Arithmetic and Memory Separation

Romain Bardou  
INRIA Saclay, France

FTfJP2008

## Introduction

Jessie

Ownership and Invariants

Problems

Our Approach

## Core Language

## Pointer Arithmetic

## Memory Separation

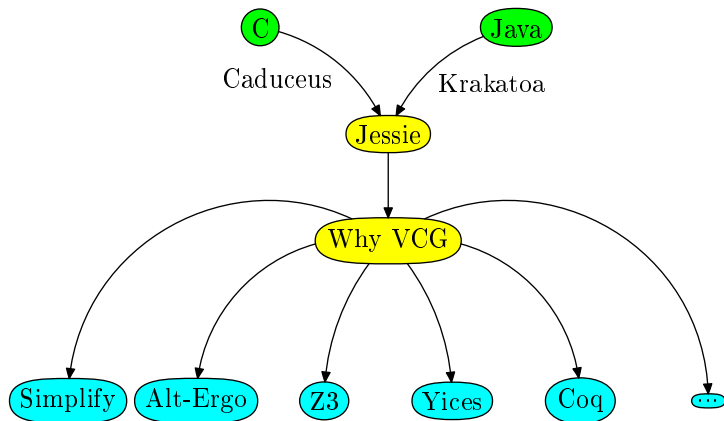
## Conclusion

# Jessie (1/2)

Context: deductive verification

INRIA Saclay: the Why platform to verify C or Java programs

## Jessie (2/2)



# Ownership and Invariants (1/2)

Examples of invariants:

- ▶  $x \neq 0$
- ▶  $t.size = length(t.data)$
- ▶ Tree  $t$  is a search tree
- ▶ Tree  $t$  is balanced

# Ownership and Invariants (2/2)

Existing systems:

- ▶ Spec# / Boogie
- ▶ Universes type system
- ▶ Capabilities
- ▶ ...

And in Jessie?

# Problems

Memory model of Jessie:

- ▶ Pointer arithmetic
  - ▶ Used to encode *arrays*
  - ▶ A single pointer may be shifted to access several others
- ▶ Memory separation
  - ▶ Memory is *split* into several maps from pointers to values
  - ▶ Simplifies pointer aliasing problems
  - ▶ Global properties of the ownership system are harder to express

# Our Approach

- ▶ Provide a small *core language* formalizing ownership and invariants
  - ▶ Captures the core ideas of ownership
  - ▶ Simple formalization usable in proofs
  - ▶ Easy to extend
    - ▶ Pointer arithmetic
- ▶ Express the *global properties* of the ownership system, *in the logic*, using *assumptions*



Introduction

Core Language

Syntax

Semantics

Example

Pointer Arithmetic

Memory Separation

Conclusion

# Syntax

$e ::=$	$v$	Values
	$x$	Variables
	<b>let</b> $x = e$ <b>in</b> $e$	Binding
	$e; e$	Sequence
	<b>while</b> $e$ <b>do</b> $e$	Turing-completion
	<b>if</b> $e$ <b>then</b> $e$ <b>else</b> $e$	Test
	<b>new</b> $\langle e; l; r \rangle$	Allocation
	$!e$	Dereferencing
	$e := e$	Assignment
	<b>pack</b> $e$	Packing
	<b>unpack</b> $e$	Unpacking

## Semantics (1/4)

Allocation ( $p$  fresh in  $\Gamma$ ):

$$\Gamma; \mathbf{new} \langle v; l; \mathbf{r} \rangle \rightarrow \Gamma, p = \langle v; l; \mathbf{r} \rangle^\circ; p$$

Assignment:

$$\Gamma, p = \langle v_1; l; \mathbf{r} \rangle^\circ; p := v_2 \rightarrow \Gamma, p = \langle v_2; l; \mathbf{r} \rangle^\circ; \mathbf{unit}$$

## Semantics (2/4)

Packing (only if  $I$  holds in  $\Gamma$ ):

$$\Gamma, \left( \begin{array}{l} p = \langle v; I; p_1 \cdots p_n \rangle^\circ \\ p_1 = R_1^\times, \cdots, p_n = R_n^\times \end{array} \right); \mathbf{pack} \ p$$

$\rightarrow$

$$\Gamma, \left( \begin{array}{l} p = \langle v; I; p_1 \cdots p_n \rangle^\times \\ p_1 = R_1^\otimes, \cdots, p_n = R_n^\otimes \end{array} \right); \mathbf{unit}$$

## Semantics (3/4)

Unpacking:

$$\Gamma, \left( \begin{array}{l} \rho = \langle v; l; p_1 \cdots p_n \rangle^\times \\ p_1 = R_1^\otimes, \dots, p_n = R_n^\otimes \end{array} \right); \mathbf{unpack} \ \rho$$

$\rightarrow$

$$\Gamma, \left( \begin{array}{l} \rho = \langle v; l; p_1 \cdots p_n \rangle^\circ \\ p_1 = R_1^\times, \dots, p_n = R_n^\times \end{array} \right); \mathbf{unit}$$

## Semantics (4/4)

Assignment can only be done on open (unpacked) pointers:

$$\Gamma, p = \langle v_1; l; \mathbf{r} \rangle^\circ; p := v_2 \rightarrow \Gamma, p = \langle v_2; l; \mathbf{r} \rangle^\circ; \text{unit}$$

This ensures that invariants are not broken.

## Example (1/2)

[Müller, challenges in Java program verification]

Let  $t$  be an array of integer of size  $n$ .

```
int i, j, count = 0;
for (i=0; i < t.length; i++)
    if (t[i] > 0) count++;
int u[] = new int[count];
for (i=0, j=0; i < n; i++)
    if (t[i] > 0) u[j++] = t[i];
```

This copies the positive elements of  $t$  in the new array  $u$ .

Problem: access  $u[j++]$  inside array bounds?

## Example (2/2)

```
let  $i$  = new  $\langle 0; \text{true}; \emptyset \rangle$  in  
let  $j$  = new  $\langle 0; \text{true}; \emptyset \rangle$  in  
let  $count$  = new  $\langle 0; (\lambda p. !p = \text{Card}\{i \mid t[i] > 0\}); t[0..n] \rangle$  in  
while  $!i \leq n$  do  
  (if  $!t[!i] > 0$  then  $count := !count + 1;$   
    $i := !i + 1$ );  
pack  $count$ ;  
let  $u$  = new  $\langle 0; \text{true}; \emptyset \rangle[!count]$  in  
 $i := 0$ ;  
while  $!i \leq n$  do  
  (if  $!t[!i] > 0$  then  $(u[!j] := !t[!i]; j := !j + 1)$ )  
   $i := !i + 1$ )
```



Introduction

Core Language

Pointer Arithmetic

- Pointer Shifting

- Extending Allocation

- Examples

Memory Separation

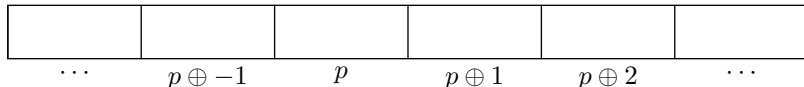
Conclusion

# Pointer Shifting

We axiomatize pointer shifting  $\oplus$ :

$$\begin{aligned} p \oplus i = p &\iff i = 0 \\ (p \oplus i) \oplus j &= p \oplus (i + j) \end{aligned}$$

Pointers do *not* have to be all related together by  $\oplus$ .



## Extending Allocation

**new**  $\lambda o. \langle v; l(o); r(o) \rangle [n]$

allocates the following fresh pointers:

$$p \oplus o = \langle v; l(o); r(o) \rangle$$

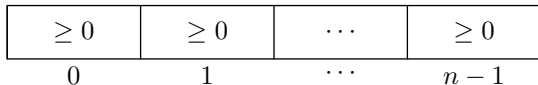
where  $o \in \{0, \dots, n-1\}$ .

All these pointers are *known to be related* by  $\oplus$ .

## Examples (1/3)

An array of positive integers:

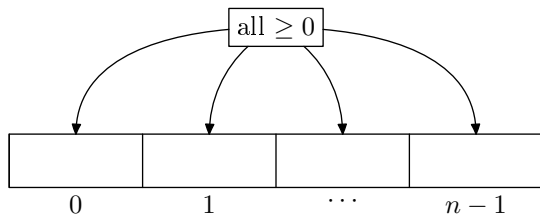
**new**  $\lambda o. \langle 0; (\lambda p. !p \geq 0); \emptyset \rangle [n]$



## Examples (2/3)

A pointer on an array of positive integers:

```
let  $p = \text{new } \lambda o. \langle 0; \text{true}; \emptyset \rangle [n]$  in  
new  $\langle 0; (\forall o, !(p \oplus o) \geq 0); p \oplus [0..(n-1)] \rangle$ 
```



## Examples (3/3)

```
let  $i = \text{new } \langle 0; \text{true}; \emptyset \rangle$  in  
let  $j = \text{new } \langle 0; \text{true}; \emptyset \rangle$  in  
let  $\text{count} = \text{new } \langle 0; (\lambda p. !p = \text{Card}\{i \mid t \oplus i > 0\}); t \oplus [0..n] \rangle$  in  
while  $!i \leq n$  do  
  (if  $!t \oplus i > 0$  then  $\text{count} := !\text{count} + 1;$   
    $i := !i + 1$ );  
pack  $\text{count};$   
let  $u = \text{new } \lambda o. \langle 0; \text{true}; \emptyset \rangle [!\text{count}]$  in  
 $i := 0;$   
while  $!i \leq n$  do  
  (if  $!t \oplus i > 0$  then  $(u \oplus !j := !t \oplus !i; j := !j + 1)$ )  
   $i := !i + 1$ )
```

Introduction

Core Language

Pointer Arithmetic

Memory Separation

- With One Heap

- With Multiple Memories

- Linking Memories

- Example

Conclusion

## With One Heap (1/3)

Global ownership properties:

- ▶  $p$  is closed  $\implies \text{Inv}(p)$
- ▶  $p$  is closed  $\implies$  reps of  $p$  are owned
- ▶ Owner of  $p$  is unique

Axioms?

Depends on the heap.

In Spec# / Boogie: *IsHeap*

$$\forall h. \text{IsHeap}(h) \implies \text{Global\_ownership\_properties}(h)$$



## With One Heap (2/3)

Another point of view: assumptions

The following code:

```
x := !y
```

becomes, at the Boogie or Why level:

```
assume Global_ownership_properties(h)  
h := store(h, x, select(h, y))  
assume Global_ownership_properties(h)
```

## With One Heap (3/3)

Suppose a free variable  $x$ .

**let**  $y = \mathbf{new}$   $\langle 0; (\lambda p. !p > !x); x \rangle$  **in**  $y := !x + 1$ ; **pack**  $y; y$

Post-condition:  $!y > !x$

Resulting proof obligation (simplified):

$$\left. \begin{array}{l} \forall h, x, y \\ \text{IsHeap}(h) \\ \text{closed}(h, y) \end{array} \right\} \implies \text{select}(h, y) > \text{select}(h, x)$$

## With Multiple Memories

The heap  $h$  is split into several maps from pointers to values.

$$\left. \begin{array}{l} \forall h_x, h_y, x, y \\ \text{IsHeap}(???) \\ \text{closed}(h_y, y) \end{array} \right\} \implies \text{select}(h_y, y) > \text{select}(h_x, x)$$

# Linking Memories (1/2)

Axiom:

$$\left. \begin{array}{l} \forall h, h_x, h_y. \\ \text{linked}(h, h_x) \\ \text{linked}(h, h_y) \\ \text{IsHeap}(h) \end{array} \right\} \implies \text{Global\_ownership\_properties}(h, h_x, h_y)$$

Proof obligation:

$$\left. \begin{array}{l} \forall h, h_x, h_y, x, y \\ \text{linked}(h, h_x) \\ \text{linked}(h, h_y) \\ \text{IsHeap}(h) \\ \text{closed}(h_y, y) \end{array} \right\} \implies \text{select}(h_y, y) > \text{select}(h_x, x)$$

This is inconsistent!

## Linking Memories (2/2)

Solution: use the assumption point of view.

...some code...

**assume** *Global\_ownership\_properties*(*Current\_heap*<sub>x</sub>, *Current\_heap*<sub>y</sub>)

...some code...

Proof obligation:

$$\left. \begin{array}{l} \forall h_x, h_y, x, y \\ \textit{Global\_ownership\_properties}(h_x, h_y) \\ \textit{closed}(h_y, y) \end{array} \right\} \Rightarrow \textit{select}(h_y, y) > \textit{select}(h_x, x)$$

## Example

...

**pack** *count*;

...

**while**  $!i \leq n$  **do**

**(if**  $!t \oplus !i > 0$  **then**  $(u \oplus !j := !t \oplus !i; j := !j + 1)$ )

$i := !i + 1$ )

Thanks to memory separation:

- ▶ Contents of array  $t$  is not modified: **trivial**

Thanks to the invariant system:

- ▶ All accesses to array  $u$  are valid: **immediate consequence of  $closed(count)$  and the assumed global ownership properties**

Introduction

Core Language

Pointer Arithmetic

Memory Separation

Conclusion

# Conclusion

The power of the ownership system of Spec#...

- ▶ captured in a small core language,
- ▶ implemented with pointer arithmetic,
- ▶ and memory separation.

Other possible extensions such as classes (implemented in Jessie).

Could be used in ESC/Java, ...